

Warm-up

1. Solve: $\frac{1}{3}x - 5(2x + 4) = 10$

$$25^{2/3}$$

2. What is another way to write $25^{1/2}$

$$\sqrt{25}$$

$$\sqrt[3]{25}$$

3. What does it mean to be a perfect square? List a few examples of perfect squares.

$$4, 9, 16, 25, \dots$$

Objective:

Today we will:

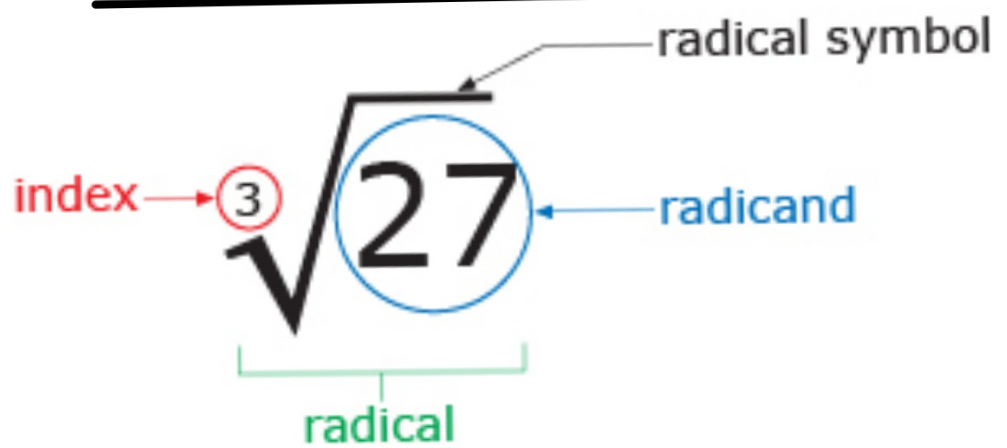
- Simplify Radicals
- Add and subtract Radicals

Agenda:

- Warm-Up and Unit 1 Intro
- Radical notes/examples
- Lesson Check
- Independent Practice

Unit 1

Parts of a Radical



* If there is no number for the index, it is a square root.

Simplifying Radicals

- Find the highest perfect square factor of the radicand
- Split into two radicals
- Simplify the perfect square radical

Ex. 1 $\sqrt{50}$

$\sqrt{25} \sqrt{2}$
 $5\sqrt{2}$

Ex. 2 $\sqrt{32}$

$\sqrt{16} \sqrt{2}$
 $4\sqrt{2}$

$\sqrt{4} \sqrt{8}$
 $2\sqrt{8}$
 $2\sqrt{4} \sqrt{2}$

$= 4\sqrt{2}$

Ex. 3 $3\sqrt{108}$

$3\sqrt{36} \sqrt{3}$
 $18\sqrt{3}$

- 4
- 9
- 16
- 25
- 36
- 49
- 64
- 81
- 100

Higher Index?

- Same Steps, except use perfect cubes, perfect 4's, 5's, etc.

Ex. 1 $\sqrt[3]{81}$

$\sqrt[3]{27} \sqrt[3]{3}$
 $(3 \sqrt[3]{3})$

$\left\{ \begin{array}{l} 8 \\ 27 \\ 64 \\ 125 \end{array} \right.$

Ex. 2

$$\sqrt[3]{500}$$

$$\sqrt[3]{125} \cdot \sqrt[3]{4}$$
$$(5 \sqrt[3]{4})$$

Ex. 3

$$\sqrt[3]{128}$$

$$\sqrt[3]{64} \cdot \sqrt[3]{2}$$
$$(4 \sqrt[3]{2})$$

$$\left\{ \begin{array}{l} 8 \\ 27 \\ 64 \\ 125 \end{array} \right.$$

Ex. 4

$$\sqrt[4]{80}$$

$$\sqrt[4]{16} \sqrt[4]{5}$$
$$(2 \sqrt[4]{5})$$

Ex. 5

$$\sqrt[5]{486}$$

$$\sqrt[5]{243} \sqrt[5]{2}$$
$$(3 \sqrt[5]{2})$$

$$\left\{ \begin{array}{l} 16 \\ 81 \\ 256 \\ 625 \end{array} \right.$$

$$\left\{ \begin{array}{l} 32 \\ 243 \\ 1024 \end{array} \right.$$

Radicals with variables

- Simplify number of radicand the same way
- List variable in groups that match the index
- Pull out as many whole groups as possible

Ex. 1

$$\sqrt[2]{18x^4y^5}$$

$$\sqrt{x}$$

$$\sqrt{9} \sqrt{2 \textcircled{xx} \textcircled{xx} \textcircled{yy} \textcircled{yy}}$$

$$3x^2y^2\sqrt{2y}$$

$$\sqrt{9} \sqrt{2x^2x^2y^2y^2}$$

$$3x^2y^2\sqrt{2y}$$

Ex. 2

$$\sqrt[2]{147x^7y^6z^2}$$

$$\sqrt{49} \quad \sqrt{\textcircled{3} \cancel{x} \cancel{x} \cancel{x} \textcircled{x} \cancel{y} \cancel{y} \cancel{y} \cancel{z}}$$

$$7x^3y^3z\sqrt{3x}$$

Ex. 3

$$\sqrt{75x^5y^8}$$

$5x^2y^4\sqrt{3x}$

$$13x^6z\sqrt{5xyz}$$

$$\sqrt{845x^{13}yz^3}$$

Ex. 4 $\sqrt[3]{16x^5y^9}$

~~$\sqrt[3]{8}$~~ ~~$\sqrt[3]{2x^2y^3y^3y^3}$~~

$2xy^3 \sqrt[3]{2x^2}$

Ex. 5 $\sqrt[4]{81x^6y^3z^5}$

~~$\sqrt[4]{81}$~~ ~~$\sqrt[4]{x^4x^2y^3z^4z}$~~

$3xz \sqrt[4]{x^2y^3z}$

Adding and Subtracting Radicals

****Can only add/sub radicals that have the same index and radicand!!**

Steps

- Simplify each radical seperately
- Combine coeffieicients with a common radical

Ex. 1 $4\sqrt{13} + 7\sqrt{13}$
 $11\sqrt{13}$

Ex. 2 $9\sqrt[3]{5x} - 12\sqrt[3]{5x} + 3\sqrt{5x}$
 $-3\sqrt[3]{5x} + 3\sqrt{5x}$

Ex. 3

$$\begin{aligned} & \sqrt{27} + \sqrt{48} \\ & \sqrt{9\sqrt{3}} \mid \sqrt{16\sqrt{3}} \\ & 3\sqrt{3} + 4\sqrt{3} \\ & 7\sqrt{3} \end{aligned}$$

Ex. 4

$$\begin{aligned} & 4\sqrt{72} + 3\sqrt{200} \\ & 4\sqrt{36\sqrt{2}} + 3\sqrt{100\sqrt{2}} \\ & 24\sqrt{2} + 30\sqrt{2} \\ & \boxed{54\sqrt{2}} \end{aligned}$$

Ex. 5

$$4\sqrt{63} - \sqrt{175}$$

$$6\sqrt{832} - 7\sqrt{637}$$

Ex. 6

$$2\sqrt[3]{24} + \sqrt[3]{32}$$

Wrap-Up

- What are the parts of the radical?
- What are the steps for simplifying radicals?
- How do we add or subtract radicals?
- Why should radical expressions be simplified?

